PEP 2017 Assignment 2

- 1) Evaluate the following integrals:
- (a) $I = \int \sqrt{x} dx$
- (b) $I = \int 3\sin^2 \cos x dx$
- (c) $I = \int \left(\frac{1}{2} 2x^2\right) dx$
- (d) $I = \int_0^1 x \sqrt{1-x} dx$ (Hint: You can evaluate it using the integration by parts)
- (e) $I = \int_0^{\pi} x^2 \sin x dx$

(2) Calculate the area bounded by the positive branch of the parabola $y^2 = 25x$, the x-axis and the ordinates where x = 0 and x = 36.

(3) Calculate the arc length of the positive branch of the curve $y^2 = (7 - x)(5 + x)$ between x = -5 and x = 1.

- (4) Calculate the volume generated by revolving the ellipse $x^2 \cdot 9 + y^2 / 25 = 1$ about the x-axis.
- (5) A hemisphere has a radius of 125mm. Calculate the position of its center of mass.