

**[Marking Scheme]**

**Theoretical Question 2**

***Motion of an Electric Dipole in a Magnetic Field***

(1)  <b>2.8</b>	1.0	(1a) ➤ 0.2 obtain correct result for the <i>total force</i> ➤ 0.2 write down the correct <i>equation of motion</i> for the <i>center of mass</i> *eq.(1) ➤ 0.2 obtain correct result for the <i>total torque</i> with respect to the center of mass ➤ 0.2 write down the correct <i>equation of motion</i> for <i>rotation</i> around the center of mass *eq.(2) ➤ 0.2 obtain correct result for the <i>moment of inertia</i> for rotation around the center of mass of the dipole *eq.(3)
	1.0	(1b) ➤ 0.5 obtain correct expression for the <i>conserved quantity</i> $\vec{P}$ *eq.(4) ➤ 0.2 knowing that <i>total kinetic energy</i> is <i>conserved</i> ➤ 0.3 obtain the correct expression for $E$ in terms of $v_{CM}$ and $\omega$ *eq.(5)
	0.8	(1c) prove that $J$ is conserved ➤ 0.3 for realizing the time derivative of $J$ is zero ➤ 0.5 for an explicit proof

(2)  7.2	1.2	(2a) <ul style="list-style-type: none"> <li>➤ 0.2 knowing to <i>use the proper conservation laws</i></li> <li>➤ 0.2 knowing to <i>use the initial condition</i> to obtain the value of the conserved quantities</li> <li>➤ 0.2 write down eq.(12) correctly</li> <li>➤ 0.4 knowing <math>\dot{\phi}</math> <i>should not vanish</i></li> <li>➤ 0.2 obtain the correct <i>expression for <math>\omega_c</math></i> *eq.(14)</li> </ul>
	3.0	(2b) <ul style="list-style-type: none"> <li>➤ 0.3 knowing to <i>use the conserved quantity J</i></li> <li>➤ 0.3 knowing to <i>use the initial condition</i> to obtain the value of <math>J</math></li> <li>➤ 0.2 knowing that <math>x_{CM} \geq 0</math></li> <li>➤ 0.2 knowing that maximum distance <math>d_m</math> is reached <i>when <math>\omega</math> takes its minimum value</i></li> <li>➤ 0.2 knowing to <i>discuss the cases <math>\omega_0 &lt; \omega_c</math>, <math>\omega_0 &gt; \omega_c</math> and <math>\omega_0 = \omega_c</math></i> *eq.(17)</li> <li>➤ 0.6 obtain the correct <i>expression of <math>d_m</math> for <math>\omega_0 &lt; \omega_c</math></i></li> <li>➤ 0.6 obtain the correct <i>expression of <math>d_m</math> for <math>\omega_0 &gt; \omega_c</math></i> *eq.(18)</li> <li>➤ 0.2 knowing that it takes infinite <i>time to reach the turning point</i> for <math>\omega_0 = \omega_c</math></li> <li>➤ 0.4 obtain the correct <i>expression of <math>d_m</math> for <math>\omega_0 = \omega_c</math></i></li> </ul>
	3.0	(3c) <ul style="list-style-type: none"> <li>➤ 0.5 write down the <i>Coulomb force term</i> correctly *eq.(20)</li> <li>➤ 0.2 knowing that <i>there is a centrifugal force</i></li> <li>➤ 0.8 write down the <i>centrifugal force term</i> correctly *eq.(21)</li> <li>➤ 0.5 knowing that <i>there is a magnetic force term</i> due to center of mass motion</li> <li>➤ 1.0 write down the <i>magnetic force term</i> correctly *eq.(22)</li> </ul>